**Historic Hotels**

**Topic**
Profit model, Optimization, and Problem Solving and Mathematical Reasoning

**Key Question**
How do you price rooms in a historic hotel to maximize profit?

**Learning Goals**
Students will:
- Use benefits and constraints to create a procedure to measure profit.
- Consider how to use and exclude data
- Represent real-world situations mathematically
- Make decisions about whether or not a solution meets the needs of a client
- Communicate the solution clearly to the client

**Recommended supplies for all MEAs**
It is recommended to have all of these supplies in a central location in the room. It is recommended to let the students know that they are available, but not to encourage them to use anything in particular.

- Rulers
- Calculators
- Whiteboards, posterboards, or other presentation tools such as a document camera
- Optional: Computers with programs such as Microsoft Word and Excel

**What are Model Eliciting Activities (MEAs)?**
Model-Eliciting Activities are problem activities explicitly designed to help students develop conceptual foundations for deeper and higher order ideas in mathematics, science, engineering, and other disciplines. Each task asks students to mathematically interpret a complex real-world situation and requires the formation of a mathematical description, procedure, or method for the purpose of making a decision for a realistic client. Because teams of students are producing a description, procedure, or method (instead of a one-word or one-number answer), students’ solutions to the task reveal explicitly how they are thinking about the given situation.

**The Historic Hotels MEA consists of four components:**
1) **Background Reading:** Students individually read the newspaper article to become familiar with the context of the problem. This handout is on page 6-7.
2) **Individual Questions:** Students individually answer these reading comprehension questions about the newspaper article to become even more familiar with the context and beginning thinking about the problem. This handout is on page 8.
3) **Historic Hotels Team Activity:** In teams of three or four, have the teams read through the problem statement and answer the team questions. Then have the teams work on the problem statement for approximately 45 minutes. The time range depends on the amount of self-reflection and revision you want the students to do. It can be shorter if you are looking for students’ first thoughts, and can be longer if you expect a polished solution and well-written letter. Each team needs the handout on page 9.
4) **Process of sharing solutions:** Each team writes their solution in a letter or memo to the client. Then, each team presents their solution to the class. Whole class discussion is intermingled with these presentations to discuss the different solutions, the mathematics involved, and the effectiveness of the different solutions in meeting the needs of the client.

In totality, each MEA takes approximately 2-3 class periods to implement, but can be shortened by having students do the individual work during out-of-class time. The Presentation Form can be useful and is explained on page 4 and found on page 9.

**Recommended Progression of the MEA**
While other implementation options are possible for MEAs, it is recommended that the MEA be implemented in a cooperative learning format. Numerous research studies have proven cooperative learning to be effective at improving student achievement, understanding, and problem solving skills. In this method students will complete work individually (Newspaper article and readiness questions; as well as initial thoughts on the problem statement) and then work together as a group. This is important because brainstorming works best when students have individual time to think before working as a group. Students can be graded on both their individual and group contributions. Social skills’ discussion at the beginning of the MEA and reflection questions at the end of the MEA are also essential aspects of cooperative learning.

Social Skills (3 - 5 minutes)
Students must be taught how to communicate and work well in groups. Several social skills that are essential to group work are decision-making, asking questions, and communicating and listening. The teacher can show part of a YouTube video and discuss aspects of these skills before beginning the MEA.
(http://www.youtube.com/user/flowmathematics)

Newspaper Article and Readiness Questions:
The purpose of the newspaper article and the readiness questions is to introduce the students to the context of the problem. (10 minutes): Give the article and the questions to the students the day before for homework. Then, in the next class, discuss as a class the answers to the readiness questions before beginning to discuss the problem statement.

Problem Statement:
You may want to read the problem statement to the students and then identify as a class: a) the client that the students are working for and b) the product that the students are being asked to produce. Once you have addressed the points above, allow the students to work on the problem statement. Let the students know that they will be sharing their solution to the rest of the class. Tell students you that you will randomly pick a group member to present for each group. Tell the students that they need to make sure that everyone understands their group’s solution so they need to be sure to work together well. The group member who will present can be picked by assigning each group member a number.

Working on the Problem Statement (35-50 minutes):
Place the students in teams of three or four. Students should begin to work by sharing their initial ideas for solving the problem. If you already use teams in your classroom, it is best if you continue with these same teams since results for MEAs are better when the students have already developed a working relationship with their team members. If you do not use teams in your classroom and classroom management is an issue, the teacher may form the teams. If classroom management is not an issue, the students may form their own teams. You may want to have the students choose a name for their team to promote unity.

Teachers’ role: As they work, your role should be one of a facilitator and observer. Avoid questions or comments that steer the students toward a particular solution. Try to answer their questions with questions so that the student teams figure out their own issues. Also during this time, try to get a sense of how the students are solving the problem so that you can ask them questions about their solutions during their presentations.

Presentations of Solutions (15-30 minutes):
The teams present their solutions to the class. There are several options of how you do this. Doing this electronically or assigning students to give feedback as out-of-class work can lessen the time spent on presentations. If you choose to do this in class, which offers the chance for the richest discussions, the following are recommendations for implementation. Each
presentation typically takes 3 – 5 minutes. You may want to limit the number of presentations to five or six or limit the number of presentations to the number of original (or significantly different) solutions to the MEA.

Before beginning the presentations, encourage the other students to not only listen to the other teams’ presentations but also to a) try to understand the other teams’ solutions and b) consider how well these other solutions meet the needs of the client. You may want to offer points to students that ask ‘good’ questions of the other teams, or you may want students to complete a reflection page (explanation – page 4, form – page 14) in which they explain how they would revise their solution after hearing about the other solutions. As students offer their presentations and ask questions, whole class discussions should be intermixed with the presentations in order to address conflicts or differences in solutions. When the presentations are over, collect the student teams’ memos/letters, presentation overheads, and any other work you would like to look over or assess.

Assessment of Students’ Work
You can decide if you wish to evaluate the students’ work. If you decide to do so, you may find the following Assessment Guide Rubric helpful:

Performance Level Effectiveness: Does the solution meet the client’s needs?
Requires redirection: The product is on the wrong track. Working longer or harder with this approach will not work. The students may need additional feedback from the teacher.
Requires major extensions or refinements: The product is a good start toward meeting the client’s needs, but a lot more work is needed to respond to all of the issues.
Requires only minor editing: The product is nearly ready for the client to use. It still needs a few small modifications, additions, or refinements.

Useful for this specific situation: No changes are necessary to meet the client’s immediate needs.
Share-able or re-usable: The tool not only works for the immediate solution, but it would be easy for others to modify and use in similar situations. OR The solution goes above and beyond meeting the immediate needs of the client.

Implementing an MEA with Students for the First Time
You may want to let students know the following about MEAs:
• MEAs are longer problems; there are no immediate answers. Instead, students should expect to work on the problem and gradually revise their solution over a period of 45 minutes to an hour.
• MEAs often have more than one solution or one way of thinking about the problem.
• Let the students know ahead of time that they will be presenting their solutions to the class. Tell them to prepare for a 3-5 minute presentation, and that they may use overhead transparencies or other visuals during their presentation.
• Let the students know that you won’t be answering questions such as “Is this the right way to do it?” or “Are we done yet?” You can tell them that you will answer clarification questions, but that you will not guide them through the MEA.
• Remind students to make sure that they have returned to the problem statement to verify that they have fully answered the question.
• If students struggle with writing the letter, encourage them to read the letter out loud to each other. This usually helps them identify omissions and errors.

Observing Students as They Work on the Historic Hotels MEA
You may find the Observation Form (page 9) useful for making notes about one or more of your teams of students as they work on the MEA. We have found that the form could be filled out “real-time” as you observe the students working
or sometime shortly after you observe the students. The form can be used to record observations about what concepts the students are using, how they are interacting as a team, how they are organizing the data, what tools they use, what revisions to their solutions they may make, and any other miscellaneous comments.

**Presentation Form** *(Optional)*
As the teams of students present their solutions to the class, you may find it helpful to have each student complete the presentation form on page 10. This form asks students to evaluate and provide feedback about the solutions of at least two teams. It also asks students to consider how they would revise their own solution to the Historic Hotels MEA after hearing of the other teams’ solutions.

**Student Reflection Form**
You may find the Student Reflection Form (page 11) useful for concluding the MEA with the students. The form is a debriefing tool, and it asks students to consider the concepts that they used in solving the MEA and to consider how they would revise their previous solution after hearing of all the different solutions presented by the various teams.

**Guiding Documents**
This activity has the potential to address these and other Grades 6-8 NCTM Mathematics Standards

**Numbers and Operations**
- work flexibly with fractions, decimals, and percents to solve problems;
- understand and use ratios and proportions to represent quantitative relationships;
- develop meaning for integers and represent and compare quantities with them;
- understand the meaning and effects of arithmetic operations with fractions, decimals, and integers;
- develop, analyze, and explain methods for solving problems involving proportions, such as scaling and finding equivalent ratios.

**Algebra**
- represent, analyze, and generalize a variety of patterns with tables, graphs, words, and, when possible, symbolic rules;
- identify functions as linear or nonlinear and contrast their properties from tables, graphs, or equations;
- model and solve contextualized problems using various representations, such as graphs, tables, and equations.

**Problem Solving**
- Build new mathematical knowledge through problem solving;
- Solve problems that arise in mathematics and in other contexts;
- Apply and adapt a variety of appropriate strategies to solve problems;
- Monitor and reflect on the process of mathematical problem solving.

**Communication**
- Organize and consolidate their mathematical thinking through communication;
- Communicate their mathematical thinking coherently and clearly to peers, teachers, and others;
- Analyze and evaluate the mathematical thinking and strategies of others;
- Use the language of mathematics to express mathematical ideas precisely.

**Connections**
- Recognize and use connections among mathematical ideas;
- Understand how mathematical ideas interconnect and build on one another to produce a coherent whole;
- Recognize and apply mathematics in contexts outside of mathematics.

**Representation**
- Create and use representations to organize, record, and communicate mathematical ideas;
- Select, apply, and translate among mathematical representations to solve problems;
- Use representations to model and interpret physical, social, and mathematical phenomena.

**Common Core Mathematics Standards**

4.OA.3 Solve multistep word problems posed with whole numbers and having whole-number answers using the four operations, including problems in which remainders must be interpreted. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.

1. 5.OA.1 Use parentheses, brackets, or braces in numerical expressions, and evaluate expressions with these symbols.

5.OA.2 Write simple expressions that record calculations with numbers, and interpret numerical expressions without evaluating them. For example, express the calculation “add 8 and 7, then multiply by 2” as \(2 \times (8 + 7)\).
Recognize that $3 \times (18932 + 921)$ is three times as large as $18932 + 921$, without having to calculate the indicated sum or product.

5.G.2 Represent real world and mathematical problems by graphing points in the first quadrant of the coordinate plane, and interpret coordinate values of points in the context of the situation.

6.EE.6 Use variables to represent numbers and write expressions when solving a real-world or mathematical problem; understand that a variable can represent an unknown number, or, depending on the purpose at hand, any number in a specified set.

7.EE.2 Understand that rewriting an expression in different forms in a problem context can shed light on the problem and how the quantities in it are related.

H.S. F-IF-4 For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity.

H.S. F-IF-7 Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.

H.S. F-BF-1 Write a function that describes a relationship between two quantities.

H.S. N-Q.1 Use units as a way to understand problems and to guide the solution of multi-step problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays. 2. Define appropriate quantities for the purpose of descriptive modeling.

H.S. A-SSE.2 Use the structure of an expression to identify ways to rewrite it.

H.S. A-CED.2 Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.

Standards for Mathematical Practices integration with MEAs

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<tr>
<th>Mathematical Practice</th>
<th>How it occurs in MEAs</th>
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<td>1. Make sense of problems and persevere in solving them.</td>
<td>As participants work through iterations of their models they continue to gain new insights into ways to use mathematics to develop their models. The structure of MEAs allows for participants to stay engaged and to have sustained problem solving experiences.</td>
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<td>2. Reason abstractly and quantitatively</td>
<td>MEAs allow participants to both contextualize, by focusing on the real world context of the situation, and decontextualize by representing a situation symbolically.</td>
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<td>3. Construct viable arguments and critique the reasoning of others.</td>
<td>Throughout MEAs while groups are working and presenting their models.</td>
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<td>4. Model with mathematics.</td>
<td>This is the essential focus of MEAs; for participants to apply the mathematics that they know to solve problems in everyday life, society, or the workplace. This is done through iterative cycles of model construction, evaluation, and revision.</td>
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<td>5. Use appropriate tools strategically.</td>
<td>Materials are made available for groups as they work on MEAs including graph paper, graphing calculators, computers, applets, dynamic software, spreadsheets, and measuring devices.</td>
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<td>6. Attend to precision.</td>
<td>Precise communication is essential in MEAs and participants develop the ability to communicate their mathematical understanding through different representations including written, verbal, symbolic, graphical, pictorial, concrete, and realistic.</td>
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<td>7. Look for and make use of structure.</td>
<td>Participants in MEAs can use their knowledge of mathematical properties and algebraic expressions to develop their solutions.</td>
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<td>8. Look for and express regularity in repeated reasoning.</td>
<td>As participants develop their models the patterns they notice can assist in their model development.</td>
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The Golden Gate Casino is Las Vegas' oldest hotel-casino still in operation. The hotel opened Jan. 13, 1906, under the name Hotel Nevada, with a hotel room rate of $1 per day. The first telephone in Las Vegas was at the golden gate with a phone number of 1. The hotel gained its current name in 1955 when a group of Italian-Americans from San Francisco Bay Area started the Golden Gate Casino.

In 2012, the Golden Gate began its first major renovation in more than 50 years. The $12 million renovation includes a 35,000-square-foot, five-story hotel tower with 14 new suites and two penthouses.

"People have a certain feel they expect from Vegas, and they get that here," Mark Brandenburg, president of the Golden Gate, said Monday.

Brandenburg still talks proudly of the Golden Gate's famous shrimp cocktail, which his stepfather, Italo Ghelfi, and his partners brought from the San Francisco Bay area and introduced in Las Vegas in 1959.

The historical aspects could be what draws people back downtown after years of billion-dollar buildings on the Strip, casino and tourism experts say. Downtown could position itself to lure repeat visitors and those willing to venture away from the larger resorts.
"With around 100 rooms, you can offer a higher level of personal experience. I'm not knocking the Strip, but people are starting to learn there are other properties in town besides the mega-resorts that can offer a Vegas experience," said Brandenburg.

"If they can add a more upscale type of an experience, downtown can draw people who may have already stayed on the Strip but are coming back looking for something new," said Seyhmus Baloglu, an assistant dean at UNLV’s Harrah Hotel College who studies tourism and marketing.

"By adding festivals, music and other special events, they can draw people who might be staying at the Aria or the Bellagio to come downtown and increase the amount of money they spend while they're here," Baloglu said.

The Smith Center for the Performing Arts and a growing arts district help provide those extras, as the downtown hotels continue to revitalize themselves.

David Schwartz, director of the UNLV Gaming Research Center, and Baloglu agree that modern makeovers of the historic properties could pay off for downtown, especially if they can deliver luxury at a more affordable price.

"If the visitor counts continue to rise, as they are projected to do, and the Strip prices go up, as they may do, then there's a real opening for downtown," Schwartz said. "But it's important that the properties follow through by giving people an experience that will keep them coming back."

References


http://en.wikipedia.org/wiki/Golden_Gate_Hotel_and_Casino
Historic Hotels Model-Eliciting Activity

READINESS QUESTIONS

Please answer these questions individually.

1. Why is the Golden Gate Casino a famous Las Vegas casino?

2. What are the benefits and negatives of renovating hotel rooms?

3. What are some responsibilities that a hotel manager might have?

4. What factors could affect the price of a hotel room?
Mark Brandenburg, president of the Golden Gate Casino, has offered your team the chance to be interns at his hotel. There are a wide variety of tasks that must be coordinated to have a well-functioning hotel. A hotel in Las Vegas needs employees with a wide variety of skills and knowledge backgrounds. However, Brandenburg recognizes that hotel management is different for casino hotels versus non-casino hotels so he would like you to learn about both types. He has a task for you that focuses on the price of the hotel rooms.

The Golden Gate Casino currently has 102 rooms. Mr. Brandenburg would like you to figure out how to make the most profit on just the hotel rooms. On a typical weekend all of the rooms are usually occupied when the daily rate is $60 per room. He has found that for every dollar increase in the daily $60 rate, one less room is rented. So, for example, if he charged $61 dollars per room, only 101 rooms would be occupied. If he charged $62, only 100 rooms would be occupied. Each occupied room has a $5 cost for service and maintenance per day.

Mr. Brandenburg would like to know how much he should charge per room in order to maximize his profit and what his profit would be at that rate. Also, he would like to have a procedure for finding the daily rate that would maximize his profit in the future even if the hotel prices and the maintenance costs change.

Write a letter to Mr. Brandenburg explaining how he can calculate his profit and how much he should charge so that his profit is maximized. Be sure that your method works even if hotel prices and costs rise in the future. Include a good reason for each step of your procedure.

Your team will also be responsible for presenting your solution, procedure, and letter to our class.

As you work with your team, keep in mind these questions.

1. Who are you working for?

2. What are you being asked to do in the problem statement?
Historic Hotels Model-Eliciting Activity

OBSERVATION FORM FOR TEACHERS

Team: __________________________

STEM (Science, Technology, Engineering, & Mathematics) Concepts Used:
What STEM concepts and skills did the students use to solve the problem?

Team Interactions:
How did the students interact within their team or share insights with each other?

Data Organization & Problem Perspective:
How did the students organize the problem data? How did the students interpret the task? What perspective did they take?

Tools:
What tools did the students use? How did they use these tools?

Miscellaneous Comments about the team functionality or the problem:

Cycles of Assessment & Justification:
How did the students question their problem-solving processes and their results? How did they justify their assumptions and results? What cycles did they go through?
PRESENTATION FORM

Name________________________________________

While the presentations are happening, choose TWO teams to evaluate. Look for things that you like about their solution and/or things that you would change in their solution. You are not evaluating their style of presenting. For example, don’t write, “They should have organized their presentation better.” Evaluate their solution only.

Team ________________________________

Strengths of their solution:

Weaknesses of their solution:

Team ________________________________

Strengths of their solution:

Weaknesses of their solution:

After seeing the other presentations, how would you change your solution? If you would not change your solution, give reasons why your solution does not need changes.
Historic Hotels Model-Eliciting Activity

STUDENT REFLECTION FORM

Name __________________________ Date________________________

1. What mathematical or scientific concepts and skills (e.g. ratios, proportions, forces, etc.) did you use to solve this problem?

2. How well did you understand the concepts you used?

   Not at all                  A little bit                  Some                  Most of it                  All of it

   Explain your choice:

3. How well did your team work together? How could you improve your teamwork?

4. Did this activity change how you think about mathematics?